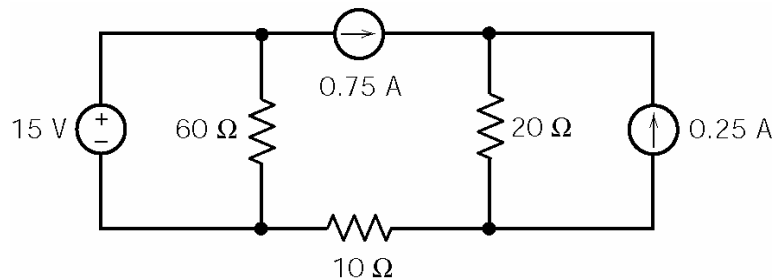


## Problem

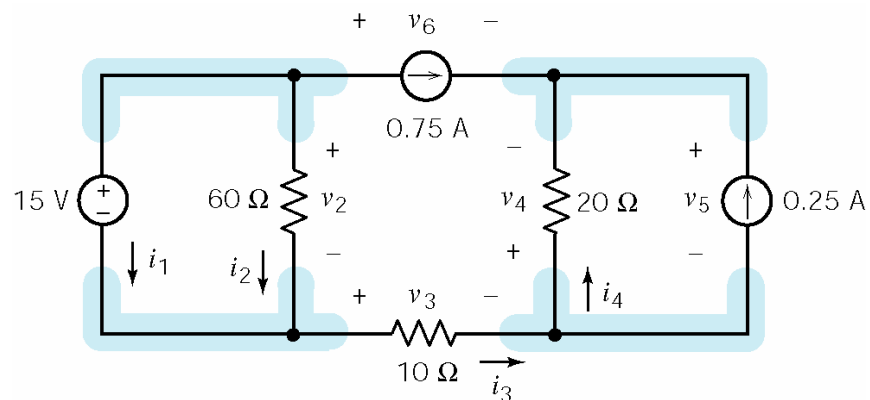
Determine the voltage and current of each of the circuit elements in this circuit.



**Hint:** You'll need to specify reference directions for the element voltages and currents. There is more than one way to do that, and your answers will depend on the reference directions that you choose.

## Solution

We can label the circuit as follows:



The subscripts suggest a numbering of the circuit elements. Apply KCL at node *b* to get

$$i_4 + 0.25 + 0.75 = 0 \Rightarrow i_4 = -1.0 \text{ A}$$

Next, apply KCL at node *d* to get

$$i_3 = i_4 + 0.25 = -1.0 + 0.25 = -0.75 \text{ A}$$

Next, apply KVL to the loop consisting of the voltage source and the 60 Ω resistor to get

$$v_2 - 15 = 0 \Rightarrow v_2 = 15 \text{ V}$$

Apply Ohm's law to each of the resistors to get

$$i_2 = \frac{v_2}{60} = \frac{15}{60} = 0.25 \text{ A},$$

$$v_3 = 10 i_3 = 10(-0.75) = -7.5 \text{ V}$$

and

$$v_4 = 20 i_4 = 20(-1) = -20 \text{ V}$$

Next, apply KCL at node  $c$  to get

$$i_1 + i_2 = i_3 = 0 \Rightarrow i_1 = i_3 - i_2 = -0.75 - 0.25 = -1.0 \text{ A}$$

Next, apply KVL to the loop consisting of the 0.75 A current source and three resistors to get

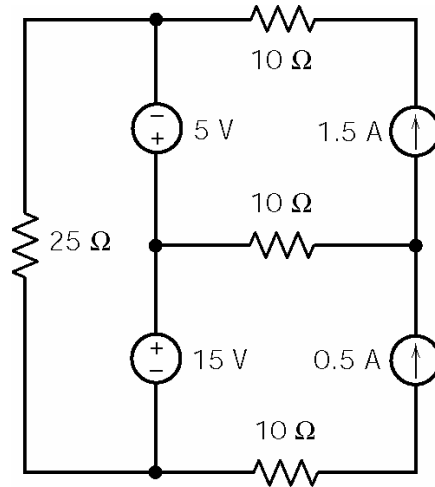
$$v_6 - v_4 - v_3 - v_2 = 0 \Rightarrow v_6 = v_4 + v_3 + v_2 = -20 + (-7.5) + 15 = -12.5 \text{ V}$$

Finally, apply KVL to the loop consisting of the 0.25 A current source and the 20  $\Omega$  resistor to get

$$v_5 + v_4 = 0 \Rightarrow v_5 = -v_4 = -(-20) = 20 \text{ V}$$

## Problem

Determine the voltage and current of each of the circuit elements in this circuit.



**Hint:** You'll need to specify reference directions for the element voltages and currents. There is more than one way to do that, and your answers will depend on the reference directions that you choose.

## Solution

We can label the circuit as follows:

The subscripts suggest a numbering of the circuit elements. Apply KCL at node  $b$  to get

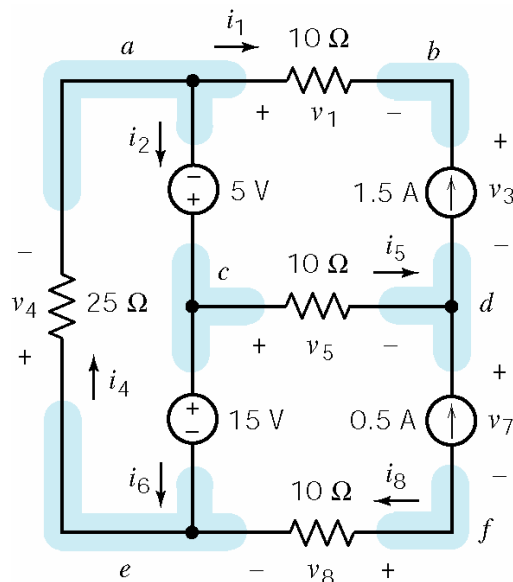
$$i_1 + 1.5 = 0 \Rightarrow i_1 = -1.5 \text{ A}$$

Apply KCL at node  $d$  to get

$$i_5 + 0.5 = 1.5 \Rightarrow i_5 = 1.0 \text{ A}$$

Apply KCL at node  $f$  to get

$$i_8 + 0.5 = 0 \Rightarrow i_8 = -0.5 \text{ A}$$



Apply Ohm's law to each of the  $10 \Omega$  resistors to get

$$v_1 = 10 i_1 = 10(-1.5) = -15 \text{ V}, \quad v_5 = 10 i_5 = 10(1) = 10 \text{ V} \quad \text{and} \quad v_8 = 10 i_8 = 10(-0.5) = -5 \text{ V}$$

Apply KVL to the loop consisting of the voltage sources and the  $25\ \Omega$  resistor to get

$$-5 + 15 + v_4 = 0 \Rightarrow v_4 = -10\ \text{V}$$

Apply Ohm's law to the  $25\ \Omega$  resistor to get

$$i_4 = \frac{v_4}{25} = \frac{-10}{25} = -0.4\ \text{A}$$

Apply KCL at node  $a$  to get

$$i_1 + i_2 = i_4 \Rightarrow i_2 = i_4 - i_1 = -0.4 - (-1.5) = 1.1\ \text{A}$$

Apply KCL at node  $e$  to get

$$i_6 + i_8 = i_4 \Rightarrow i_6 = i_4 - i_8 = -0.4 - (-0.5) = 0.1\ \text{A}$$

Apply KVL to the loop consisting of the  $1.5\ \text{A}$  current source, the  $5\ \text{V}$  voltage source and two  $10\ \Omega$  resistors to get

$$v_1 + v_3 - v_5 + 5 = 0 \Rightarrow v_3 = -5 + v_5 - v_1 = -5 + 10 - (-15) = 20\ \text{V}$$

Finally, apply KVL to the loop consisting of the  $0.5\ \text{A}$  current source, the  $15\ \text{V}$  voltage source and two  $10\ \Omega$  resistors to get

$$v_7 + v_8 - 15 + v_5 = 0 \Rightarrow v_7 = 15 - (v_5 + v_8) = 15 - (10 + (-5)) = 10\ \text{V}$$